

4.

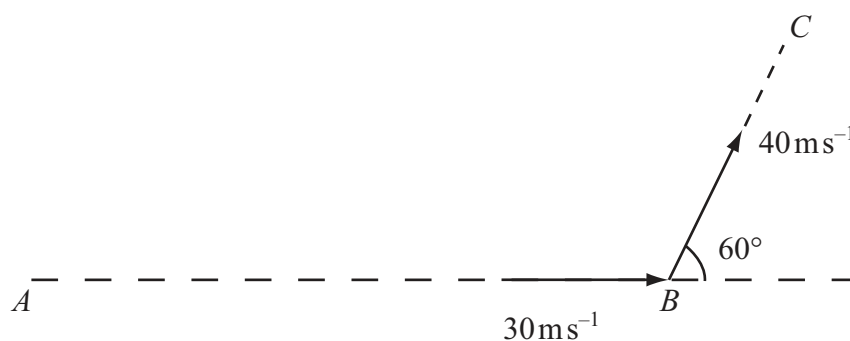


Figure 1

The points A , B and C lie in a horizontal plane. A batsman strikes a ball of mass 0.25 kg . Immediately before being struck, the ball is moving along the horizontal line AB with speed 30 ms^{-1} . Immediately after being struck, the ball moves along the horizontal line BC with speed 40 ms^{-1} . The line BC makes an angle of 60° with the original direction of motion AB , as shown in Figure 1.

Find, to 3 significant figures,

- (i) the magnitude of the impulse given to the ball,
- (ii) the size of the angle that the direction of this impulse makes with the original direction of motion AB .

(8)



5. A cyclist and her bicycle have a total mass of 70 kg. She cycles along a straight horizontal road with constant speed 3.5 m s^{-1} . She is working at a constant rate of 490 W.

(a) Find the magnitude of the resistance to motion. (4)

The cyclist now cycles down a straight road which is inclined at an angle θ to the horizontal, where $\sin \theta = \frac{1}{14}$, at a constant speed $U \text{ m s}^{-1}$. The magnitude of the non-gravitational resistance to motion is modelled as $40U$ newtons. She is now working at a constant rate of 24 W.

(b) Find the value of U . (7)

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Question 5 continued

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Question 5 continued

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(Total 11 marks)

Q5

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6.

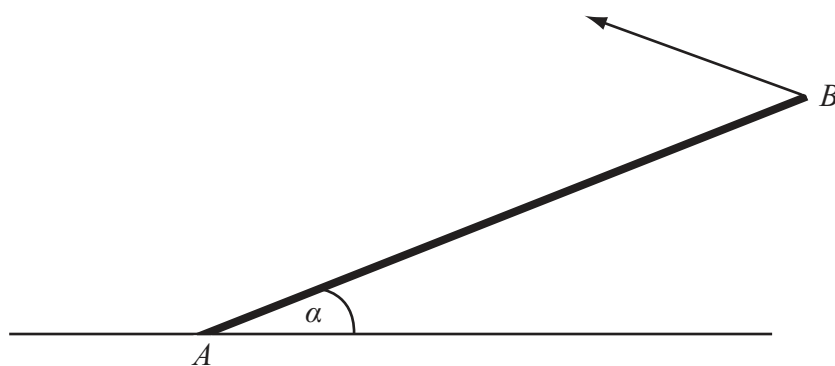


Figure 2

A uniform rod AB , of mass 20 kg and length 4 m, rests with one end A on rough horizontal ground. The rod is held in limiting equilibrium at an angle α to the horizontal, where $\tan \alpha = \frac{3}{4}$, by a force acting at B , as shown in Figure 2. The line of action of this force lies in the vertical plane which contains the rod. The coefficient of friction between the ground and the rod is 0.5. Find the magnitude of the normal reaction of the ground on the rod at A .
(7)



Question 6 continued

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7. [The centre of mass of a semi-circular lamina of radius r is $\frac{4r}{3\pi}$ from the centre]

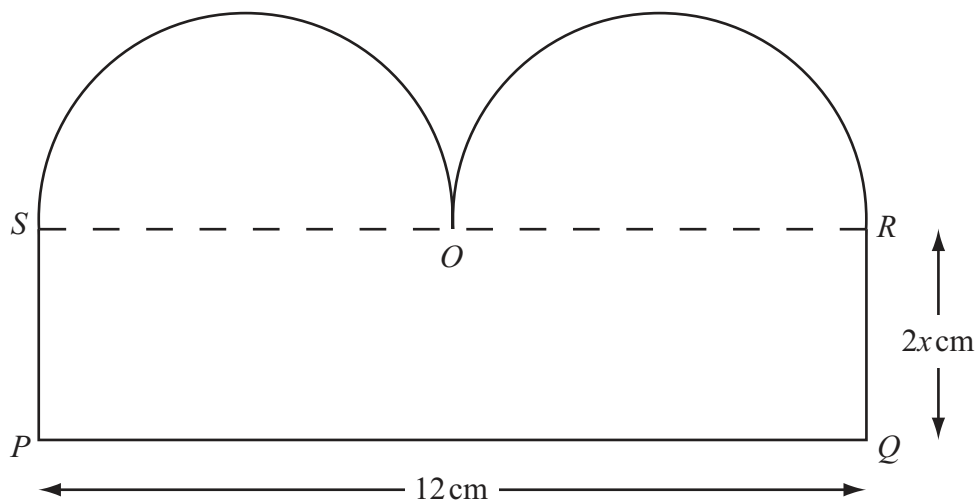


Figure 3

A template T consists of a uniform plane lamina $PQROS$, as shown in Figure 3. The lamina is bounded by two semicircles, with diameters SO and OR , and by the sides SP , PQ and QR of the rectangle $PQRS$. The point O is the mid-point of SR , $PQ = 12$ cm and $QR = 2x$ cm.

(a) Show that the centre of mass of T is a distance $\frac{4|2x^2 - 3|}{8x + 3\pi}$ cm from SR . (7)

The template T is freely suspended from the point P and hangs in equilibrium.

Given that $x = 2$ and that θ is the angle that PQ makes with the horizontal,

(b) show that $\tan \theta = \frac{48 + 9\pi}{22 + 6\pi}$. (4)



8. [In this question \mathbf{i} and \mathbf{j} are unit vectors in a horizontal and upward vertical direction respectively]

A particle P is projected from a fixed point O on horizontal ground with velocity $u(\mathbf{i} + c\mathbf{j})\text{ms}^{-1}$, where c and u are positive constants. The particle moves freely under gravity until it strikes the ground at A , where it immediately comes to rest. Relative to O , the position vector of a point on the path of P is $(x\mathbf{i} + y\mathbf{j})\text{m}$.

- (a) Show that

$$y = cx - \frac{4.9x^2}{u^2}. \quad (5)$$

Given that $u = 7$, $OA = R\text{m}$ and the maximum vertical height of P above the ground is $H\text{m}$,

- (b) using the result in part (a), or otherwise, find, in terms of c ,

(i) R

(ii) H .

(6)

Given also that when P is at the point Q , the velocity of P is at right angles to its initial velocity,

- (c) find, in terms of c , the value of x at Q .

(6)



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Question 8 continued

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Question 8 continued

Q8

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(Total 17 marks)

TOTAL FOR PAPER: 75 MARKS

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